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6-4 Additional Practice

Logarithmic Functions

Graph each function and identify the domain, range, x-intercept, y-intercept, asymptote, and end behavior. Compare each graph to the parent function.

1.
$$f(x) = \log_{\Delta}(x-2) + 2$$

domain:

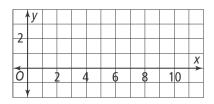
range:

x-intercept:

y-intercept:

asymptote:

end behavior:



Find the inverse of each function.

2.
$$f(x) = 6 \log_5(2x-6)$$

2.
$$f(x) = 6 \log_5(2x - 6)$$
 3. $f(x) = 2 \log_{0.5}(-5x) + 4$ **4.** $f(x) = \ln 3^x - 2$

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$$f(x) = \ln 3^x - 2$$

- **5.** A hurricane center uses the function $s = 95\log d + 75$ to relate the wind speed in miles per hour s and distance in miles d a hurricane travels. How many miles will the hurricane travel with a wind speed of approximately 320 mph?
- **6.** Which company's profit shows a greater average rate of change? Company A: \$1.5 million profit in 2010; after 5 years, grew exponentially to \$2.5 million. Company B: profit modeled by $P(B) = 1.3(1.15)^{X}$

6-4 Additional Practice

Logarithmic Functions

Graph the function below and identify the domain, range, x-intercept, y-intercept, asymptote, and end behavior. Compare the graph to the parent function.

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1.
$$f(x) = \log_{\Delta}(x-2) + 2$$

domain: $\{x | x > 2\}$

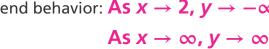
range: all real numbers

x-intercept: $2\frac{1}{16}$

y-intercept: **none**

asymptote: x = 2

end behavior: As $x \to 2$, $y \to -\infty$



The graph is shifted right 2 units and up 2 units.

Find the inverse of each function.

2.
$$f(x) = 6 \log_5(2x - 6)$$

2.
$$f(x) = 6 \log_5(2x - 6)$$
 3. $f(x) = 2 \log_{0.5}(-5x) + 4$

4.
$$f(x) = \ln 3^x - 2$$

$$f^{-1}(x) = \frac{1}{2}(5\frac{x}{6} + 6)$$

$$f^{-1}(x) = \frac{1}{2}(5\frac{x}{6} + 6)$$
 $f^{-1}(x) = -\frac{1}{5}(0.5\frac{x-4}{2})$ $f^{-1}(x) = \frac{e^{x+2}}{3}$

$$f^{-1}(x)=\frac{e^{x+2}}{3}$$

5. A hurricane center uses the function $s = 95 \log d + 75$ to relate the wind speed in miles per hour s and distance in miles d a hurricane travels. How many miles will the hurricane travel with a wind speed of approximately 320 mph?

$$320 = 95 \log d + 75$$

$$d \approx 10^{2.58} \approx 380 \text{ mi}$$

6. Which company's profit shows a greater average rate of change between 2010 and 2015?

Company A: \$1.5 million profit in 2010; after 5 years, grew exponentially to \$2.5 million.

Company B: profit, in million of dollars, modeled by $P(B) = 1.3(1.15)^{x}$, where x is the number of years after the end of 2010.

Company A: 0.2 million per year; Company B: about 0.26 million per year; Company B has greater average rate of change.