# PRACTICE & PROBLEM SOLVING





#### UNDERSTAND

- **18.** Construct Arguments Justice found that the fifth root of  $243x^{15}y^5$  is  $3x^3y$ . Is Justice correct? Explain your reasoning.
- **19.** Make Sense and Persevere For a show, each sphere was inflated to have a volume of  $4,186\frac{2}{3}$  in.<sup>3</sup> Explain how to find the radius *r* of one of the inflated spheres. Use technology to compute your answer.



**20. Error Analysis** Describe and correct the error a student made in writing this exponential expression in radical form.

$$x^{\frac{4}{3}} = (x^{4})^{\frac{1}{3}}$$
$$(x^{4})^{\frac{1}{3}} = \sqrt[4]{x^{3}} \qquad \checkmark$$

- **21.** Construct Arguments Determine whether  $\sqrt[3]{x^2}$  is equal to  $(\sqrt[3]{x})^2$ . Explain your reasoning.
- **22. Use Structure** How many third roots does –512 have? Explain your reasoning.
- **23. Higher Order Thinking** The annual interest formula below calculates the final balance of an account, *F*, given a starting balance, *S*, and an interest rate, *r*, after 10 years.

$$F=S(1+r)^{10}$$

When solving for *r*, why can the negative root be ignored?

24. Mathematical Connections The lengths of the two legs of a right triangle are 4 and 8. What is the length of the hypotenuse, in simplest radical form?

### PRACTICE

Find the specified roots of each number. SEE EXAMPLE 1

- 25. the real fourth roots of 81
- 26. the real third roots of 343
- 27. the real fifth roots of 1,024
- 28. the real square roots of 25

Rewrite each expression using a fractional exponent. SEE EXAMPLE 2

<b>29.</b> <sup>4</sup> √16 <sup>2</sup>	<b>30.</b> ∜729
<b>31.</b> $\sqrt[7]{x^2}$	<b>32.</b> ∜ab

What is the value of each expression? Round to the nearest hundredth if necessary. SEE EXAMPLE 3 33.  $\sqrt[4]{25^2}$  34.  $-\sqrt[3]{125^5}$ 

Simplify each expression. SEE EXAMPLE 4

<b>35.</b> <sup>3</sup> √8y <sup>9</sup>	<b>36.</b> ∜q <sup>12</sup> z <sup>4</sup>
<b>37</b> . ∜729a <sup>24</sup> b <sup>18</sup>	<b>38.</b> ∜√ <sup>8</sup> g <sup>40</sup>

Solve each equation. SEE EXAMPLE 5

**39.**  $1,125 = 9x^3$  **40.**  $6,480 = 5w^4$ 

- **41.**  $270 = 10q^3$  **42.**  $256 = 4h^6$
- **43.** A small cube has the volume shown. Its side length is 1.5 in. less than a second, larger cube. What is the volume of the larger cube? SEE EXAMPLE 6



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# APPLY

**44. Model With Mathematics** A water-walking ball has a volume of approximately 4.19 m<sup>3</sup>. What is the radius, *r*, of the ball?



**45. Make Sense and Persevere** Ahmed received a box of gifts. The box is a rectangular prism with the same height and width, and the length is twice the width. The volume of the box is 3,456 in.<sup>3</sup>. What is the height of the box?



**46.** Make Sense and Persevere Amelia's bank account earns interest annually. The equation shows her starting balance of \$200 and her balance at the end of four years, \$220.82. At what rate, *r*, did Amelia earn interest?

$$220.82 = 200(1 + r)^4$$

**47.** Model With Mathematics One measure of a patient's body surface area is found using the expression  $\sqrt{\frac{H \bullet W}{3,600}}$ . Write this with a fractional exponent.

### SSESSMENT PRACTICE

**48.** Determine if each expression is another way to write  $b^{\frac{3}{4}}$ . Select *Yes* or *No*.

	Yes	No
<b>a</b> . $\sqrt[4]{b^3}$		
<b>b.</b> ( <i>b</i> <sup>3</sup> ) <sup>1/4</sup>		
<b>c</b> . $b^{\frac{4}{3}}$		
d. $\sqrt[3]{b^4}$		
e. $\frac{b^3}{b^4}$		

- **49.** SAT/ACT Which of the following is equivalent to  $\sqrt[6]{4,096x^{18}y^{30}}$ , where x > 0 and y > 0?
  - (a)  $682.7x^{15}y^{24}$ (b)  $4x^{1.6}y^{1.8}$ (c)  $4,096x^3y^5$ (c)  $4x^3y^5$ (c)  $682.7x^3y^5$
- **50.** Performance Task A milk processing company uses cylindrical-shaped containers. The height of the container is equal to the diameter of the base.



**Part A** The volume of one container is about 169.65 ft<sup>3</sup>. How much material is needed to make the lateral surface of the shipping container?

**Part B** The cargo hold of a ship is 20 ft high. What is the largest number of these shipping containers that could be stacked on top of each other inside the cargo hold?

