



**UNDERSTAND**

9. **Reason** Explain how to find the range of the inverse of  $f(x) = \sqrt{2x - 3}$  without finding  $f^{-1}(x)$ .
10. **Error Analysis** Describe and correct the error a student made in finding the inverse of the function  $f(x) = x^2 - 4$ .

$$f(x) = x^2 - 4$$

$$x = y^2 - 4$$

$$\sqrt{x} = \sqrt{y^2 - 4}$$

$$\sqrt{x} = y - 2$$

$$\sqrt{x} + 2 = y$$

$$f^{-1}(x) = \sqrt{x} + 2$$
X

11. **Higher Order Thinking** What is the inverse operation of raising a number to the 4th power? How can you use the inverse operation of a number raised to the 4th power to find the inverse of the function  $f(x) = x^4 - 1$ ? Is the inverse of  $f$  a function? Explain.
12. **Communicate Precisely** A function has the ordered pairs (1, 3), (7, 4), (8, 6), and (9, y). What restrictions are there on the value of  $y$  so that the inverse of the function is also a function? Explain.
13. **Construct Arguments** What is the inverse of the function  $a(b) = \frac{1}{4}b^2$ ? Show how to use composition of functions to prove you found the correct inverse.
14. **Construct Arguments** A relation has one element in its domain and two elements in its range. Is the relation a function? Is the inverse of the relation a function? Explain.
15. **Mathematical Connections** Find the  $x$ - and  $y$ -intercepts of the function  $y = 2x + 1$ . What are the intercepts of the inverse function? How are the intercepts related?

**PRACTICE**

Identify the inverse relation. Is it a function?

SEE EXAMPLE 1

16.

|     |    |    |    |   |    |   |
|-----|----|----|----|---|----|---|
| $x$ | -2 | -1 | 0  | 1 | 2  | 3 |
| $y$ | 9  | 3  | -4 | 8 | -6 | 3 |

17.

|     |    |   |   |    |   |   |
|-----|----|---|---|----|---|---|
| $x$ | -2 | 1 | 0 | 1  | 2 | 3 |
| $y$ | -7 | 6 | 8 | -1 | 3 | 7 |

Write an equation to represent the inverse of  $f$ . Sketch the graphs of  $f$ ,  $y = x$ , and the inverse of  $f$  on the same coordinate axes. Is the inverse of  $f$  a function? SEE EXAMPLE 2

18. Let  $f(x) = x + 3$ .      19. Let  $f(x) = 4x - 1$ .
20. Let  $f(x) = x^2 + 1$ .      21. Let  $f(x) = \sqrt{x + 5}$ .

Find the inverse of the function by identifying an appropriate restriction of its domain. SEE EXAMPLE 3

22.  $f(x) = x^2 + 4x + 4$       23.  $f(x) = x^2 - 6x + 9$
24.  $f(x) = x^2 - 2$       25.  $f(x) = x^2 + 5$

Find an equation of the inverse function, and state the domain of the inverse. SEE EXAMPLE 4

26.  $f(x) = 2x^2 - 5$       27.  $f(x) = \sqrt{x + 6}$
28.  $f(x) = 3x + 10$       29.  $f(x) = \sqrt{x - 9}$

Use composition to determine whether  $f$  and  $g$  are inverse functions. SEE EXAMPLE 5

30.  $f(x) = 2x - 9$ ,  $g(x) = \frac{1}{2}x + 9$
31.  $f(x) = \sqrt{\frac{x+4}{3}}$ ,  $g(x) = 3x^2 - 4$

32. A manager purchased cones for ice cream. Find a formula for the length of the radius,  $r$ , of a cone in terms of its volume,  $V$ . Then find the length of the radius of a cone if the volume is  $290\pi \text{ cm}^3$  and the height is 15 cm. SEE EXAMPLE 6

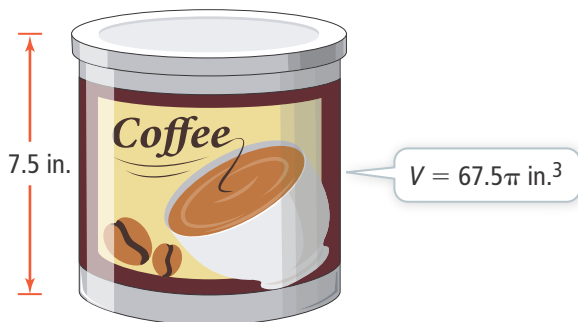


**APPLY**

33. **Model With Mathematics** The formula for converting Celsius to Fahrenheit is  $F = \frac{5}{9}(C - 32)$ . Find the inverse formula, and use it to find the Celsius temperature when the Fahrenheit temperature is  $56^\circ\text{F}$ .
34. **Reason** A DJ charges an hourly fee and an equipment setup fee.



- a. Write a function for the cost,  $C$ , of hiring a DJ for  $n$  hours.
- b. Find the inverse of the cost function. What does the function represent?
- c. If the DJ charged \$550, for how many hours was she hired? Use the inverse function.
35. **Reason** A coffee can is in the shape of a cylinder.



- a. Find the formula that gives the radius of the coffee can  $r$  in terms of the volume  $V$  and height  $h$ .
- b. Describe any restrictions on the formula.
- c. What is the radius of a coffee can given the volume is  $67.5\pi \text{ in.}^3$  and the height is  $7.5 \text{ in.}$ ?

**ASSESSMENT PRACTICE**

36. Choose Yes or No to tell whether each function has an inverse that is a function.

|                            | Yes                      | No                       |
|----------------------------|--------------------------|--------------------------|
| a. $f(x) = 2x - 9$         | <input type="checkbox"/> | <input type="checkbox"/> |
| b. $f(x) = x^2 + 4$        | <input type="checkbox"/> | <input type="checkbox"/> |
| c. $f(x) = x^3 - 6$        | <input type="checkbox"/> | <input type="checkbox"/> |
| d. $f(x) = \sqrt{2x + 7}$  | <input type="checkbox"/> | <input type="checkbox"/> |
| e. $f(x) = x^2 - 10x + 25$ | <input type="checkbox"/> | <input type="checkbox"/> |

37. **SAT/ACT** What is the range of the inverse of  $f(x) = \sqrt{-ax + b} - c$ , where  $a$ ,  $b$ , and  $c$  are real numbers?
- (A)  $y \geq \frac{a}{b}$
- (B)  $y \leq \frac{b}{a}$
- (C)  $y \geq -\frac{a}{b}$
- (D)  $y \geq -\frac{b}{a}$
- (E)  $y \geq c$

38. **Performance Task** The table shows several functions and some of the inverses of those functions. The table also shows whether some of the inverses are functions.

| Function     | Inverse                   | Is the inverse a function? |
|--------------|---------------------------|----------------------------|
| $f(x) = x$   | $f^{-1}(x) = x$           | yes                        |
| $g(x) = x^2$ | $g^{-1}(x) = \pm\sqrt{x}$ | no                         |
| $h(x) = x^3$ | $h^{-1}(x) = \sqrt[3]{x}$ | yes                        |
| $k(x) = x^4$ |                           |                            |
| $m(x) = x^5$ |                           |                            |
| $n(x) = x^6$ |                           |                            |

**Part A** Determine the inverses of the remaining functions in the table.

**Part B** Determine if the inverses of the remaining functions in the table are functions.

**Part C** Make a conjecture about the power of a function if the inverse of that function is a function.